#### A Compiler for Lazy ML

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#### Abstract

LML is a strongly typed, statically scoped functional language with lazy evaluation. It is compiled trough a number of program transformations which makes the code generation easier. Code is generated in two steps, first code for an abstract graph manipulation machine, the G-machine. From this code machine code is generated. Some benchmark tests are also presented.

# 1. Introduction

The LML compiler project is an attempt to produce efficient code for a functional language with lazy evaluation for an ordinary von Neumann machine. When we started we knew of no other attempt to do this, but since then some similiar things have appeared like [Huda84], and [Fair82]. There are several compilers for non-lazy functional languages, eg. [Card84].

The LML compiler is written in LML and it produces (as an intermediate step) G-code, code for an abstract graph manipulation machine, from which machine code generation is fairly easy. This makes the LML compiler easy to port to other machines.

The approach used in the compiler is to perform many transformation on the program ("source to source" transformations) to get a program for which generation of efficient code is less complicated.

The execution of the program is based on graph-reduction. The graph represents the expression that is evaluated, and it is transformed until it is in a printable

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form. During execution there is also an ordinary stack on which computations are performed (as in ordinary languages) when this can be done without violating the lazy evaluation semantics.

# 2. LML Language Description

Lazy ML, or LML for short, is a lazy and completely functional variant of ML, [Miln84] and [Gord79]. The syntax used here is slightly different from Standard ML. The main differences between LML and ML is that LML has lazy evaluation, there are no references type nor assignments and no exception-mechanism; strings are lists of characters, and there are no explicit input/output procedures.

An LML program is an expression whose value is printed when the program is executed.

Function definitions may use pattern matching, which makes programs both easier to write and understand. Such a definition contains a number of equations for a function separated by ||, e.g.

Pattern matching can also be used to bind multiple values like 'let  $(a,b) = f \times in'$ . There is also a case expression to do pattern matching.

An important concept in LML is local definitions. A local definition has the form tet D in e' where D is a declarator to T. In a let expression the declarator defines the meaning of a number of identifiers that can be used in the expression part of the let.

- \* Appendix A describes the terminology used in the following descriptions.
- \*\* Declarator syntax is described in appendix B.

# 2.1 Pattern matching semantics

All pattern matching is translated into case expressions (as described below), so this explanation need only concern the semantics of case expressions.

The case expression is evaluated by finding the first pattern that matches. The patterns are check from top to bottom, and each patters is checked from left to right. The checking is stopped as soon as a subpart fails to match. This rather explicit top-down, left-right ordering is perhaps unfortunate, but some ordering must be imposed to avoid the necessity of parallel evaluation of the subparts of the expression that is to be matched.

#### 2.2 Type definitions

It is possible to define new types in LML, the mechanism for this is very similar to the one proposed for Standard ML (SML). The type definitions resemble those of Hope, [Burs80]. It would be possible to have no predefined types (except the function type) and instead let the user define all types. This would give the same performance as having them predefined, except for the integers which are implemented with the machine arithmetic.

A new type is introduced by

`let type T in e'

where T is a type declarator, which is similar to an ordinary declarator, ie. it can be

'T<sub>1</sub> and T<sub>2</sub>' mutual definition

'rec T' recursive definition.

`i(v<sub>1</sub>, ...v<sub>n</sub>)=C<sub>1</sub>(t<sub>11</sub>, ... t<sub>1</sub>)+... C<sub>m</sub>(...)'
where i is the name of the
new type and v<sub>1</sub>... are type
variables, C<sub>1</sub>...C<sub>n</sub> are the
new constructors, t<sub>n</sub> are
type expression possibly

containing v... Using this the booleans could be defined by

let type bool = true + false in

3-tuples let type tuple3(\*a, \*b, \*c) = T3(\*a, \*b, \*c)

and lists by

let type rec list(\*a) =
 nil + cons(\*a, list(\*a)) in

(To make things more readable nullary constructors are written without `()'.) All of these are predefined are of course predefined.

There is a difference in type definitions between LML and Standard ML. In SML all constructors take either zero or one argument. To get more arguments a tuple must be used instead; so the list definition would be

```
let type rec list(*a) =
  nil + cons(*a # list(*a)) in
```

('#' is used for cartesian product.) This means that a list on cons form may be formed by 'cons e' where 'e' is any expression of the right type. We have not adopted this for two reasons:

- it requires tupels to be predefined, we can define them in the language.
- since we have lazy evaluation the domain for eg. lists would be different from the intuitive lazy list domain. It would be possible to have lists of the form 'cons ⊥', ie. a list known to be on cons form but nevertheless without head and tail part, since there is a difference between ⊥ and (1,⊥) using our case semantics.

It is of course still possible to define the types as in SML.

When a type is introduced the new constructors, ie. the names introduced on the right, may be used to form expressions of that type. An expression 'C<sub>k</sub>(e<sub>1</sub>,...)' is a canonical value in the new type. A canonical value is something which yields itself as value when evaluated.

The new constructors may also be used to form patterns. The pattern matching is the only way to take apart an expression of the new type.

### Compilation

This section describes the different passes of the compiler.

#### 3.1 Parsing

The parsing is done with a ordinary recursive descent parser which builds an abstract syntax tree. This representation is then used in the compiler until the code generation.

# 3.2 Scope analysis

The scope analysis (or renaming) assign unique names to all identifiers in the

program and checks that thee scope rules are obeyed. Giving unique names to the identifiers simplifies subsequent transformations of the program since parts of the program can now be moved around without the risk for name clashes.

Some rewriting of the syntax tree are also made, because some syntactic constructions are ambigous without further information about the symbols involved. They can only be resolved when the meaning of the identifiers are known, eg. `let s = e in e'. If `s' is defined as a constructor in this scope then `s' is a pattern otherwise this is a normal variable binding.

The scope analysis traverses the tree and keeps a symbol table of the identifiers in the current scope, the tree is rebuilt where necessary.

#### 3.3 Type checking

The type checking is the based on the algorithm described in [Miln781, but extended to handle the pattern matching. The typechecker (or typededucer) deduces the most general type of each subexpression and checks that they are used consistently. The deduced types are also used later on in the code generation.

The type checking eliminates the need to do runtime type checking, since at that run time we know that the program is type correct.

### 3.4 Pattern matching transformation

The purpose of the transformations described here is to reduce all pattern matching to case expressions containing only simple patters. A simple pattern has the form 'C(i<sub>1</sub> ... i<sub>n</sub>)' (where i<sub>k</sub> are variables), it's called simple because this is the basic pattern form and it's also easy to generate code for.

All constants in the predefined types (such as true and 5) are treated as constructors in their corresponding types and they are now written with parenthesis to indicate their special status (not to confuse them with variables). This means that a pattern is built up only from constructors and variables.

There are three different kind of pattern matching beside the case expression and they are all transformed into case. First, the declarator for function definitions is transformed from

$$f p_{11} \cdots p_{1n} = e_1$$
||  $f p_{m1} \cdots p_{mn} = e_m$ 

f I<sub>1</sub> ... I<sub>n</sub> = case tuple 
$$(I_1, ..., I_n)$$
 in tuple  $(p_{11}, ..., p_{1n})$  : e<sub>1</sub> tuple  $(p_{m1}, ..., p_{mn})$  : e<sub>m</sub>

where tuple is the n-tuple constructor.

In the the second kind of matching, the value binding, there is a declarator  $\dot{\ }$  p = e'. This declarator is replaced by

where  $i_1$ , ... and  $i_n$  are the variables in the pattern p.

This declarator binds the same variables as the original one, but uses only case-matching. The reason behind this seemingly complex transformation is to preserve all properties of the declarator, it may for instance be prefixed by 'rec' to make it recursive. This works for the transformed declarator as well. Eg. the expression 'let rec (a,b) = f a in b' would be transformed to

The introduced case expressions can be viewed as selector functions to select the different parts of the expression and the recursion is still possible since bindings are "lazy".

Third, in the case of a lambda pattern (ie. '\p.e' where p is not a variable) it is transformed into '\I.let p = I in e'.

When all these transformations have been applied, there is only case pattern matching left. These must now be changed into simple patterns, ie. into expressions of the form

where the last entry may be missing if all constructors are present in the other entries. This last entry, with a single variable as the pattern, will be called the <u>default</u> entry.

The algorithm to transform complex patterns into simple patterns is as follows:

- a. Sort the patterns by the outermost constructor and group those with the same constructor together.
- b. Each of the groups is now expanded if it is not a single simple pattern. New variables are introduced for the subparts of the constructor and an expression with nested casing of those variables (with the corresponding parts of the original patterns as the new patterns) is used as the right hand side.
- c. This process is now repeated for all the new case expressions until only simple patterns are left.

This description is simplified as it does not state how to handle failures to match. In fact every new case expression must also have a default entry to handle this. To make compilation to G-code efficient we have to introduce two new constructions used in expressions (they are only used internally by the compiler): IDEF and ODEF. IDEF stands for the same value as the default entry of the nearest enclosing case (it's only used in non-default entries), ODEF means the same value as the default entry of the second nearest enclosing case (used only in default entries).

### An example:

Or with the uniform notation

Sort, group, introduce new variables, and expand cases

Since the inner of the introduced cases is nonexhaustive a default entry is introduced. The degenerate case (only a default entry) is changed to eliminate the case.

(e\_[I\_2/t] means e\_ where each free occurence of t has been changed to I\_2.)

Repeat with innermost case.

As in the example, complex patterns may be transformed into quite large simple patterns. This does not seem to be much of a

problem in practice, since most patterns used in ordinary programs are simple or almost simple. Other transformations can be used to keep the size down, eg. if large constants (ie. patterns with only constructors) are matched this may be transformed into ordinary equality comparison, thus saving space (but not execution time).

#### 3.5 Other transformations

The transformations described here operates on declarators (and makes them simpler).

All let-expressions are transformed into one of two forms

`let  $\mathbf{D}_1$  and  $\mathbf{D}_2$  ... and  $\mathbf{D}_n$  in e' or `let rec  $\mathbf{D}_1$  and  $\mathbf{D}_2$  ... and  $\mathbf{D}_n$  in e'

where each  $D_k$  has the form 'i = e'.

Function definitions are transformed from

Local declarators can now removed by:
`let local D<sub>1</sub> in D<sub>2</sub> in e' becomes
`let D<sub>3</sub> in let D<sub>2</sub> in e'
because of the renaming which made all
identifiers unique. Having unique identifiers means that pulling D<sub>1</sub> out does not
violate any scope rules (any names defined
in D<sub>4</sub> are not used in e).

All let bindings can then be flattened out to the form above.

### 3.6 Lambda lifting

The input to the code generator should be an expression of the form

where each e may begin with a number of lambdas, but must otherwise contain no lambda-expressions. The only free variables in each e must be the predefined functions or one of the f.s. Furthermore the expression 'e' must not contain any lambdas. The expression may still contain 'let' and 'let rec' -expressions.

The purpose of the lambda lifting is to lift out all lambda expression to the outermost level, which is the only place were thay may occur in the final expression. Any lambda expression not containing any free variables can simply be moved to the global level, so the main work of the lambda lifting is to remove free variables. This elimination of free variables is analogous the the abstraction used with

combinators in [Turn79] and supercombinators in [Hugh82] except we do not enforce "fully lazyness" (see [Hugh82] for details). The elimination is done by passing each free variable as an argument, and adding the corresponding parameter, to the function in which it is used. A simple example of lambda lifting is shown below.

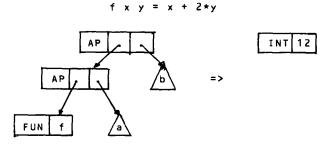
(c)
global definition: f = \y.\x.x
expression: let x = 5
 in f x 3

#### 3.7 Code generation

The abstract machine and the code generation is described in detail in [John84] and will only be briefly outlined here.

The code generation is performed in two steps. First code for an abstract machine, the G-machine, is generated and then from this code, the G-code, machine code for the specific machine (in our case the VAX11) is generated.

Code is generated separately for each definition in the global definition list. The purpose of the code for a function is that when given a graph, corresponding to the left hand side of the definition, transform this to the canonical value corresponding to the right hand side. This is in contrast to most other approaches to lazy evaluation with graph reduction where the returned value may be non-canonical and the evaluation must proceed after a function has returned (cf. [Turn791).



the graph  $\triangle$  has the canonical value 2 and  $\triangle$  the value 5.

As shown in figure 1, the code for f will, when given the first graph, transform it into the second graph.

A program is executed by doing EVAL (and printing) of the expression part of the program. EVAL always searches down the spine of the graph until a function node is found, while going down pointers to the spine nodes are pushed so that they are easily accessible to the function (this is called unwinding). The function code is then invoked and when it returns (to the caller of EVAL) it has transformed a piece of the graph to canonical form.

As said above purpose of the code for the function is to produce the canonical value of the right hand side, and so there must be a code generation scheme to produce code which computes the value. But often the unevaluated expression must be used, eg. when passing parameters or as arguments to constructors, so there must also be a code generation scheme that will produce the graph for an expression. These schemes are called E and C respectively. The compilation is rule based, there are rules for how to compile the different variants of the syntax tree for each of the code generation schemes, see figure 2 for some (simplified) rules.

```
CEil
                   = PUSHINT i
CExT
                  = PUSH n
CEcons(x,y)]
                  = CEyl; CExl; CONS
= CEyl; CExl; MKAP
CEx yl
ECx1
                   = PUSH n; EVAL
                  = E[x]; GET; E[y]; GET;
E[mul x y?
                            MUL; MKINT
                  = E[x]; HD; EVAL
E[hd x]
E[x y]
                  = CEx y?; EVAL
E[if x then y else z] =
         E[x]; GET; JFALSE L1;
E[y]; JUMP L2; L1: E[z]; L2:
```

Figure 2

By propagating the E scheme in the right way a lot of the produced code is for computing a value and not building a graph. The if expression, for instance, for which the value is wanted generates code that first evaluates the condition and then jumps to the code for the 'then' or 'else' branch. The code there will produce the value of the corresponding expressions.

#### An example:

fac n = if n = 0 then 1
 else n\*fac(n-1)

would give the code

fac:PUSH 1; EVAL; PUSHINT 0; GET; EQ;
 JFALSE L1; PUSHINT 1; JUMP L2;
L1: PUSH 1; EVAL; GET;
 PUSHINT 1; PUSH 2; PUSHFUN sub; MKAP;
 MKAP; PUSHFUN fac; MKAP; EVAL;
 GET; MUL; MKINT; JUMP L3;
L2: UPDATE 2; RET 1;

The PUSH instruction pushes a value from

the pointer stack on top of the pointer stack, the number indicates the offset from the current stack pointer. EVAL causes the graph pointed to by the pointer stack top to be evaluated. PUSHBASIC pushes a constant of the value stack. PUSHINT pushes a reference to a constant on the pointer stack. GET transfers the value pointed out by the pointer stack top to the value stack. MKAP pushes a reference to application node containing two entries from the pointer stack. EQ, MUL etc. operate on the value stack. UPDATE updates a node in the graph.

#### 3.8 Improvements

There are a number of thing that can are done to improve the code. Many of these imprivements are made by instroducing several different code generation schemes used in different contexts (eg. for return value computation, compataion of values on the value stack).

- By keeping track of what variables have already been evaluated in a certain context unnecessary EVAL instructions are avoided thereby saving time.
- When all arguments to an integer operation, for which a graph building code should be produced, are already evaluated the operation is performed in line instead. This is safe except for overflow and division by zero, but we do not handle those anyway.
- By using the type information some calculations can be simplified, eg. if two integers are compared the code for this can be emitted in line instead of calling a general value comparator.
- "Tail-call" elimination, ie. when the last thing in the code for a function is a call to another function this is done by rearranging the stack and doing a jump. This achieves tailrecursion elimination as a special case.
- When the value of an application is needed the graph corresponding to this is not built, instead the function is called the stack set up as if it would have looked if called with EVAL.

The code for the else part of the factorial function in the example above becomes:

PUSH 1; GET; PUSH 1; GET; PUSHBASIC 1; SUB; MKINT; CALLFUN fac; MUL;

instead of the previous longer and slower code.

#### 3.9 Machine code generation

Machine code generation from the G-code is rather straightforward since the G-code is

well suited for execution on a von Neumann machine. A simple code generator would just do macro-expansion" of the G-code; each G-instruction is replaced by a fixed piece of machine code. We use a more elaborate code generator which tries to avoid stack references and thereby memory references.

### 3.9.1 Node layout

In the current implementation each node has a tag field of one word followed by 0, 1, or 2 more words. The tag serves two purposes, first it indicates if the node has canonical form or not and second it tells the garbage collector how to treat the rest of the node. The tag part is not just a small number as is often the case in other implementations, but instead its an address into the machine code. By jumping to this address with different offsets different things can be done with the node, such as evaluation, garbage collection and printing. The evaluation of a node is accomplished by making a subroutine call to a certain offset from the tag, if the node is already on canonical form this address will contain a return instruction which then immediately returns, otherwise it will contain code to initiate the unwinding.

### 3.9.2 Memory allocation

Memory for the graph is allocated on a heap. Garbage collection is performed by copying the used part of the heap into another equally sized area.

During execution one machine register always points at the next free heap location, allocation of a cell is done by simply adding the cell size to the register. Heap overflow need not be tested before every allocation, instead it's tested once before a number of consecutive allocations. This brings down the allocation overhead. A normal (whatever that is) program allocates about 300 kbytes/sec.

The copying garbage collection used has some advantages:

- cells of varying sizes are easily handled.
- storage gets compacted at garbage collection, which is important when using virtual memory.
- the time spent in g.c. is proportional to the size of the used part of the heap, not the size of the heap as with mark-scan. This is important since the memory allocation is very large compared to the size of the used memory.

### 4. Current state of the compiler

The compiler as described here is not fully implemented at the moment. We have an older version of the compiler which does not do the case transformations described, but is otherwise very similar.

After completing the compiler we would like to test some other possible improvements:

- A global analysis to detect when call-by-value could be used instead of call-by-need has been proposed in EMycr807. This could bring down the amount of graph construction further.
- Vector nodes, ie. nodes with many parts of the same kind, could be used to store tuples in an efficient way.

#### 5. Performance

All benchmarks below, and the code shown in the appendicies are produced with the older version of the compiler (see above).

It is difficult to do fair comparisons between different languages, but we have tried some benchmark programs with different compilers and interpreters. If not stated otherwise the same algorith has been used for all languages, this means that even the C and Pascal programs use lists if the functional program does. Of course this is not "fair" since one would not write the an imperative program this way, but if one starts using different versions for different languages this makes the comparison even more difficult. Nevertheless, in two examples, 8queen and kwic, the programs in Pascal and C have been written in an imperative style.

All execution times given i table 1 are in seconds of CPU time (garbage collection included).

### Language processors:

- LML The lazy ML compiler described in this paper. Lazy evaluation.
- ML The ML/LCF system from Edinburgh, translates ML to LISP and interprets the LISP. Strict evaluation.
- ML-C The compiling ML system by Luca Cardelli, translates to VAX-code. Strict evaluation.
- SASL Turners SASL, translates SASL into SECD code and interprets it. Lazy evaluation.
- LISP Interpreted Franz Lisp on UNIX. Strict evaluation.

			T	able 1.				
8queen fib20 primes	LML 3.2 0.83 0.5	ML 170 46 29	ML-C 9.0 0.5 1.2	SASL 170 31 20	LISP 48 21 7.8	Liszt 5.2 1.1 1.1	Pascal 1.0 0.92	C 0.4 0.46
insort tak kwic	0.37 10 39	15 309	1.0	12 - -	6.4 76	0.8 3.0	2.6 9.7	1.8

		Table 2.		
	allocated memory (K)	max used (K)	heap size (K)	GC time (%)
fib20	45	0.3	20	4
prime	88	1.7	10	5
insort	59	4	10	15
8queen	687	6.4	50	6

Liszt Compiled Franz Lisp on UNIX. Strict evaluation.

Pascal The VAX/UNIX Pascal compiler pc. Strict evaluation.

C The VAX/UNIX C compiler cc. Strict evaluation.

#### Programs:

8queen Counting the number of solutions to the 8 queen problem (actually 7 queens are used to limit the execution time). The Pascal and C versions of this program are coded differently (coded in a nonfunctional style).

fib20 Computation of the 20th Fibonacci number.

primes The first 300 primes using Erathostene's sieve.

insort Insertion sort of 100 elements in a list (repeated 10 times).

tak The tak function with arguments 18,12,6.

kwic Keyword in context, all significant rotations of a number of sentences sorted. The Pascal program was written in the usual Pascal style with arrays.

We have also performed some measurements of memory consumption (of the LML programs) which are presented in table 2.

allocated memory: is total amount of memory allocated by the program.

max used: is maximum amount of heap memory in use at any time, ie. the part of the heap not containg garbage.

heap size: is the size of the heap (twice this amount used because of the way the garbage collector works.)

GC time: is the time spent in garbage collection.

### 6. Acknowledgements

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D. A. Turner, "New Implementation Techniques for Applicative 'rec D' makes the bindings in D recursive, [Turn79] ie. the variables bound in D may be used in the right hand sides of D. Languages", Software - Practice and Experience, Vol. 9 pp. 31-49 (1979). 'local  $\mathbf{D}_1$  in  $\mathbf{D}_2$ ' makes  $\mathbf{D}_1$  available in  $\mathbf{D}_2$ , but not outside  $\mathbf{D}_2$ . Appendix A, Terminology 'p = e' binds the variables in the pattern p to the corresponding parts of e. Program parts will (almost) always be enclosed in . . Certain names inside ip<sub>11</sub>...p<sub>1n</sub>=e<sub>1</sub> stand for special things:

tions.

|| ip  $_{1}$ ---p = e defines the function i by a number of equa-

# Appendix C, Some benchmark programs

are constructors.

C,Ck

are variables (ie. identifiers

that are not constructors).

```
let nsoln nq =
        letrec ok [] * true
            | | ok (x.1) =
                letrec safe x d [] = true
|| safe x d (q.1) = x ~= q & x ~= q+d &
                                        x ~= q-d & safe x (d+1) 1
                        safe x 1 1
                in
        in
        letrec gen 0 = [[]]
            || gen n = concmap (\\b.(filter ok (map (\\q.q.b) (count 1 nq)))) (gen (n-1))
                length (gen nq)
in
       nsoln (stoi (hd argv))
Count the number of solutions of the n-queen problem (placing n
queens on a n*n board).
Used functions:
      - apply a function to all elements of a list.
concmap - as map but concatenate the instead of cons.
length - gives the length of a list.
count - generate a list of consecutive numbers between two limits.
       - stringto integer.
stoi
      - list of arguments to the program.
argv
```

```
letrec fib n =
                                                                   Note:
                                                                          Zep is an alias for r10, used as stack pointer for the
          if n < 2 then 1
                                                                           pointer stack.
         else fib (n-1) + fib (n-2)
                                                                           The is an alias for rli, used as heap pointer.
ſn
          fib 20
                                                                    Vax assebler code:
The 20:th fibonacci number.
                                                                   # Code for function filter
                                                                           .globl C_filter
letrec tak x y z =
                                                                   C filter:
                   if (y < x) then z
                                                                   CLt100: .long
                                                                           .asclz
                                                                                    filter"
                            tak (tak (x-1) y z)
                                                                                   $CLt 100, r0
                                                                           mov1
                                 (tak (y-1) z x)
                                                                           rsb
                                 (tak (z-1) x y)
                                                                                   .byte 0,0,0,0,0
                                                                           rsb;
ín
                                                                            gæţ
                                                                                   funprinterr
          tak 18 12 6
                                                                           jmp
                                                                                   2h
                                                                                  F_filter
                                                                           .globl
                                                                   F filter:
                                                                                                  Entry point for call via EVAL
The tak function.
                                                                   FLt 100:
                                                                           subl3
                                                                                   Zep,(sp),r0
                                                                           cmp1
                                                                                   r0,$16
                                                                                   1f
                                                                           bgeq
let mod x y = x - (x/y*y) in
                                                                                   return
                                                                           jmp
let rec filter p 1 = if null 1 then []
                         else
                                                                   DLt100:
                            if mod (hd 1) p = 0 then
                                                                           .globl D_filter
                                                                   D filter:
                                                                                                  Entry point for "direct" call
                                      filter p (tl 1)
                            else
                                      hd 1 . filter p (tl 1)
                                                                                   12(Zep),r0
                                                                                                  PUSH 3
          count a b = if a > b then []
and
                                                                           mov1
                                                                                   (r0),rl
                                                                                                  EVAL
                        else a . count (a+1) b
                                                                           1sb
                                                                                   eval(rl)
                                                                                                  NULL: JFALSE L105
                                                                                   $CONS,(r0)
in
                                                                           cmp1
                                                                           jegl
                                                                                   L105
letrec sieve 1 = if null 1 then nil
                    else hd l . sieve (filter (hd 1) (tl 1))
                                                                           movl
                                                                                   (sp)+,Zep
                                                                                                  RET_NIL
                                                                           movi
                                                                                   (Zep)+,r0
let primesto n = sieve (count 2 n)
                                                                           mov1
                                                                                   $F_nil,(r0)
in
                                                                           rsb
                                                                   L105:
                                                                                                  LABEL L105
primesto 300
                                                                                                  Enough heap left?
                                                                           cmpl
                                                                                   %hp,ehp
                                                                           bleq
Generating primes up to a limit.
                                                                                  GARBMIN
                                                                                                  no: collect garbage
                                                                           jsb
    Appendix P, G-code and VAX-code
                                                                   ı:
                                                                                                  E ERUS
                                                                                   12(Zep),r2
    This is the essential part of the run time
                                                                                  4(r0),r2
$APPLY,(Zhp)+
                                                                           movl
    machinery of all programs:
                                                                           movl
                                                                                                  PUSH 2; MKAP
                                                                           movl
                                                                                   4(Zep),(Zhp)+
                                   this is were eval
                   APPLY_eval
            jmp
                                                                                   r2,(Zhp)+
                                                                           mov1
                                     of an APPLY jumps
            jmp
                   ....
                                                                           moval
                                                                                   -12(Zhp),r0
            ÍMP
                                                                           mov1
                                                                                   (r0),rl
                                                                                                  EVAL
    APPLY:
                   (%ep),r0
                                   get pointer to apply
           movl
                                                                                  eval(r1)
4(r0)
                   8(r0),-(Zep)
4(r0),r0
                                                                           jsb
                                   push argument part
            movl
                                                                                                  JFALSE L106
                                                                           tstl
                                   get function part
            movl
                                                                                  Lì06
                                                                           jeql
                   r0,-(%ep)
                                   and push it
            mov1
                    *(r0)
                                   jump via UNWIND tag
            jap
                                                                           cmpl
                                                                                  Zhp,ehp
    APPLY_eval:
                                                                           bleq
            movl
                   r0,-(%ep)
                                   push node pointer
                                                                                  GARBMIN
                                                                           jsb
                                   save current ep
                   Zep,-(sp)
APPLY
            movl
                                                                   l:
                                   enter unwind state
            ibr
 Function definition:
                                                                           movl
                                                                                  12(Zep).r2
                                                                                                  PUSH 3
                                                                                  4(r2),r2
$APPLY,(Zhp)+
                                                                           movl
          filter p L =
                                                                           movl
                                                                                                 PUSH 2; PUSHFUN filter; MKAP
                                                                                  $C_filter,(Zhp)+
                                                                           movl
                    if null L then
                                                                           mov1
                                                                                  4(%ep),(hp)+
                                                                                  $APPLY,(Zhp)+
                                                                          mov1
                                                                                                  MKAP
                    else if p (hd L) then
                                                                                  -16(Zhp),(Zhp)+
                                                                          moval
                             (hd L) . filter p (tl L)
                                                                                  r2,(Zhp)+
                                                                          movl
                                                                           movl
                                                                                  12(Zep),r2
                                                                                                  PUSH
                    el se
                                                                          movl
                                                                                  4(r2),r2
                             filter p (tl L)
 G-machine code:
                                                                          movl
                                                                                  (sp)+,rl
                                                                                                 CONS; UPDATE 5; RET 4
                                                                          movl
                                                                                  (rl),r0
                                                                          mov1
                                                                                  $CONS,(r0)
PUSH 3; EVAL; NULL; JFALSE 105;
                                                                          movl
                                                                                  r2.4(r0)
         RET NIL;
                                                                                  -12(hp),8(r0)
                                                                          moval
LABEL 105:
                                                                          movl
                                                                                  rl,%ep
PUSH 3; HD; PUSH 2; MKAP; EVAL; GET; JFALSE 106;
                                                                          rsb
         PUSH 3; TL; PUSH 2; PUSHFUN filter; MKAP; MKAP:
                                                                          movl
                                                                                  12(%ep).r2
                                                                                                  PUSH 3
         PUSH 4; HD; CONS; UPDATE 5; RET 4;
                                                                                  8(r2),12(%ep)
                                                                          movl
                                                                                                 TL; MOVE 4
LABEL 106;
                                                                          jmp
                                                                                  D filter
                                                                                                  JFUN filter
         PUSH 3; TL; MOVE 4; JFUN filter.
```